

Annex 2 Methodologies

Banking stability map and indicator

The banking stability map and indicator presents an overall assessment of changes in underlying conditions and risk factors that have a bearing on the stability of the banking sector during a period. The ratios used for constructing each composite index are given in Table 1.

Dimension	Ratios			
Soundness	CRAR #	Tier-I Capital to Tier-II Capital #	Leverage ratio as Total-Assets to Capital and Reserves	
Asset-Quality	Net NPAs to Total-Advances	Gross NPAs to Total-Advances	Sub-Standard-advances to gross NPAs #	Restructured-Standard-Advances to Standard-Advances
Profitability	Return on Assets #	Net Interest Margin #	Growth in Profit #	
Liquidity	Liquid-Assets to Total-Assets #	Customer-Deposits to Total-Assets #	Non-Bank-Advances to Customer-Deposits	Deposits maturing within-1-year to Total Deposits
Efficiency	Cost to Income	Business (Credit + Deposits) to staff expenses #		Staff Expenses to Total Expenses

Note: # Negatively related to risk.

The five composite indices represent the five dimensions of soundness, asset-quality, profitability, liquidity and efficiency. Each composite index, representing a dimension of bank functioning, takes values between zero (minimum) and 1 (maximum). Each index is a relative measure during the sample period used for its construction, where a high value means the risk in that dimension is high. Therefore, an increase in the value of the index in any particular dimension indicates an increase in risk in that dimension for that period as compared to other periods. For each ratio used for a dimension, a weighted average for the banking sector is derived, where the weights are the ratio of individual bank assets to total banking system assets. Each index is normalised for the sample period as 'ratio-on-a-given-date minus minimum-value-in-sample-period divided by maximum-value-in-sample-period minus minimum-value-in-sample-period'. A composite index of each dimension is calculated as a weighted average of normalised ratios used for that dimension where the weights are based on the marks assigned for assessment for the CAMELS rating. Based on the individual composite index for each dimension, the banking stability indicator is constructed as a simple average of these five composite indices.

Estimation of losses: Expected losses, unexpected losses and expected shortfalls of SCBs

The following standard definitions were used for estimating these losses:

Expected Loss (EL) : EL is the average credit loss that the banking system expects from its credit exposure.

Unexpected Loss (UL) : UL at 100(1- α) per cent level of significance is the loss that may occur at the α -quantile of the loss distribution.

Expected Shortfall (ES) : When the distributions of loss (Z) are continuous, expected shortfall at the 100(1- α) per cent confidence level ($ES_{\alpha}(Z)$) is defined as, $ES_{\alpha}(Z) = E[Z | Z \geq \text{VaR}_{\alpha}(Z)]$. Hence, Expected Shortfall is the conditional expectation of loss given that the loss is beyond the VaR level.

These losses were estimated as: $\text{Loss} = \text{PD} \times \text{LGD} \times \text{EAD}$

Where, EAD = Exposure at Default, is the total advances of the banking system. EAD includes only on-balance sheet items as PD was derived only for on-balance sheet exposures.

LGD = Loss Given Default. Under the baseline scenario, the average LGD was taken as 60 per cent as per the RBI guidelines on 'Capital Adequacy - The IRB Approach to Calculate Capital Requirement for Credit Risk'. LGD was taken at 65 per cent and 70 per cent under medium and severe macroeconomic conditions respectively.

PD = Probability of Default. PD was defined as gross non-performing advances to total advances ratio. Because of unavailability of data on a number of default accounts, the size of default accounts (that is, the GNPA amount) was used for derivation of PDs.

The losses, EL, UL and ES, were estimated by using a simulated PD distribution. As a first step an empirical distribution of the PD was estimated using the Kernel Density Estimate; second using the empirically estimated probability density function, 20,000 random numbers were drawn based on the Monte Carlo simulation and finally, EL, UL and ES were calculated by taking PDs as average PD, 99.9 per cent VaR of PD and average PD beyond 99.9 per cent loss region respectively.

Macro stress testing

To ascertain the resilience of banks against macroeconomic shocks, a macro stress test for credit risk was conducted. Here, the credit risk indicator was modelled as a function of macroeconomic variables, using various econometric models that relate the banking system aggregate to macroeconomic variables. The time series econometric models used were: (i) multivariate regression to model system level slippage ratio; (ii) VAR to model system level slippage ratio; (iii) quantile regression to model system level slippage ratio; (iv) multivariate regression to model bank group-wise slippage ratio data; (v) VAR to model bank group-wise slippage ratio data; and (vi) multivariate regressions for sectoral GNPA. The banking system aggregates include current and lagged values of slippage ratio, while macroeconomic variables include GDP growth, weighted average lending rate (WALR), CPI (combined) inflation, exports-to-GDP ratio ($\frac{Ex}{GDP}$), gross fiscal deficit-to-GDP ratio ($\frac{GFD}{GDP}$) and REER.

While multivariate regression allows evaluating the impact of selected macroeconomic variables on the banking system's GNPA and capital, the VAR model reflects the impact of the overall economic stress situation on the banks' capital and GNPA ratios, which also take into account the feedback effect. In these methods, the conditional mean of slippage¹ ratio is estimated and it is assumed that the impact of macro-variables on credit quality will remain the same irrespective of the level of the credit quality, which may not always be true. In order to relax this assumption, quantile regression was adapted to project credit quality, in which, in place of conditional mean the conditional quantile was estimated.

The Modelling Framework

The following multivariate models were run to estimate the impact of macroeconomic shocks on the GNPA ratio/slippage ratio (SR):

System Level Models

The projection of system level GNPA was done using three different but complementary econometric models: multivariate regression, vector autoregressive (which takes into account the feedback impact of credit quality to

¹ Slippages are fresh accretion to NPAs during a period. Slippage Ratio = Fresh NPAs/Standard Advances at the beginning of the period.

macro-variables and interaction effects) and quantile regression (which can deal with tail risks and takes into account the non-linear impact of macroeconomic shocks). The average of projections derived from these models was used for calculating the impact on CRAR.

- *Multivariate Regression*

The analysis was carried out on the slippage ratio at the aggregate level for the commercial banking system as a whole.

$$SR_t = \alpha_1 + \beta_1 SR_{t-1} - \beta_2 \Delta GDP_{t-3} + \beta_3 WALR_{t-1} - \beta_4 \left(\frac{EX}{GDP} \right)_{t-2} + \beta_5 \Delta CPI_{t-1} + \beta_6 \left(\frac{GFD}{GDP} \right)_{t-1} - \beta_7 \ln(REER)_{t-1}$$

Where, $\alpha_1, \beta_1, \beta_2, \beta_3, \beta_4, \beta_5, \beta_6$ and $\beta_7 > 0$.

- *Vector auto regression (VAR)*

In notational form, mean-adjusted VAR of order p (VAR(p)) can be written as:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + u_t ; t=0,1,2,3,\dots$$

Where, $y_t = (y_{1t}, \dots, y_{kt})'$ is a $(K \times 1)$ vector of variables at time t, the $A_i (i=1,2,\dots,p)$ are fixed $(K \times K)$ coefficient matrices and $u_t = (u_{1t}, \dots, u_{kt})'$ is a K-dimensional white noise or innovation process.

In order to estimate the VAR system, slippage ratio, WALR, CPI (combined) inflation, real GDP growth, gross fiscal deficit-to-GDP ratio and REER were selected. The appropriate order of VAR was selected based on minimum information criteria as well as other diagnostics and suitable order was found to be 2. Accordingly, VAR of order 2 (VAR(2)) was estimated and the stability of the model was checked based on roots of AR characteristic polynomial. Since all roots are found to be inside the unit circle, this selected model was found to fulfil the stability condition. The impact of various macroeconomic shocks was determined using the impulse response function of the selected VAR.

- *Quantile Regression*

In order to estimate the slippage ratio at the desired level of the conditional quantile, the following quantile regression at median (which is the present quantile of the slippage ratio) was used:

$$SR_t = \alpha_1 - \beta_1 SR_{t-1} - \beta_2 \Delta GDP_{t-3} + \beta_3 WALR_{t-1} - \beta_4 \left(\frac{EX}{GDP} \right)_{t-2} + \beta_5 \Delta CPI_{t-1} + \beta_6 \left(\frac{GFD}{GDP} \right)_{t-2}$$

Where, $\alpha_1, \beta_1, \beta_2, \beta_3, \beta_4, \beta_5$ and $\beta_6 > 0$.

Bank group level models

The projection of bank groups-wise GNPA are done using two different but complementary econometric models: multivariate regression and vector autoregressive. The average of projections derived from these models was used to calculate the impact on CRAR.

- *Multivariate regression*

In order to model the slippage ratio of various bank groups, the following multivariate regressions for different bank groups were used:

Public Sector Banks:

$$SR_t = \alpha_1 - \beta_1 SR_{t-1} - \beta_2 \Delta GDP_{t-2} + \beta_3 WALR_{t-1} - \beta_4 (\Delta REER)_{t-3} + \beta_5 \Delta CPI_{t-1} + \beta_6 \left(\frac{GFD}{GDP} \right)_{t-2}$$

Private Sector Banks:

$$SR_t = \alpha_1 - \beta_1 SR_{t-1} - \beta_2 \Delta GDP_{t-1} + \beta_3 RWALR_{t-2} - \beta_4 (\Delta REER)_{t-3} - \beta_5 \left(\frac{EX}{GDP} \right)_{t-1}$$

Foreign Banks:

$$SR_t = \alpha_1 - \beta_1 SR_{t-1} + \beta_2 WALR_{t-2} - \beta_3 (\Delta REER)_{t-1} + \beta_4 \Delta CPI_{t-1} - \beta_5 \left(\frac{EX}{GDP} \right)_{t-1} + \beta_6 \text{Dummy}$$

- *Vector auto regression*

In order to model the slippage ratio of various bank groups, different VAR models of different orders were estimated based on the following macro variables:

Public Sector Banks: Real GDP growth, CPI (combined)-inflation, WALR and first difference of REER and GFD to GDP ratio of order 2.

Private Sector Banks: Real GDP growth, real WALR and first difference of REER of order 1.

Foreign Banks: CPI (combined)-inflation, WALR and REER of order 2.

Sector level models

- *Sectoral multivariate regression*

The impact of macroeconomic shocks on various sectors was assessed by employing multivariate regression models using the aggregate GNPA ratio for each sector separately. The dependent variables consisted of lagged GNPA, sectoral GDP growth, CPI (combined)-inflation and WALR.

Impact of exchange rate movement on asset quality

The impact of the exchange rate on the asset quality of SCBs was captured through REER (36 currencies trade based using CPI inflation) which was found to be small. This could be because of merchandise export to GDP ratio and CPI in a way subsumes the effect of REER. Substituting REER with other indicators also did not improve the results.

Estimation of GNPA from slippages

Derivation of GNPA from slippage ratios, which were projected from the earlier mentioned credit risk econometric models, were based on the following assumptions: credit growth of 15 per cent; recovery rate of 9.6 per cent, 6.7 per cent, 5.8 per cent and 5.2 per cent during March, June, September and December quarters respectively; write-off rates of 6.3 per cent, 4.4 per cent, 2.8 per cent and 4.8 per cent during March, June, September and December respectively.

Projection of PAT

There are various components of profit after tax (PAT) of banks like interest income, other income, operating expenses and provisions. Hence, these components are projected using different time series econometric models (as given later) and finally PAT was estimated using the following identity:

$$PAT = NII + OOI - OE - Provisions - Income Tax$$

where, NII is Net Interest Income, OOI is Other Operating Income and OE is Operating Expenses.

- *Net Interest Income (NII)*: NII which is the difference between interest income and interest expenses is projected using the following regression equation:

$$LNII_t = -\alpha_1 + \beta_1 \times LNII_{t-1} + \beta_2 \times LNGDP_SA_{t-1} + \beta_3 \times Adv_Gr_{t-1} + \beta_4 \times Spread_t$$

where, $\alpha_1, \beta_1, \beta_2, \beta_3$, and $\beta_4 > 0$, LNII is log of NII. LNGDP_SA is seasonally adjusted log of nominal GDP at factor cost. Adv_Gr is the y-o-y growth rate of advances. Spread is the difference between average interest rate earned by interest earning assets and average interest paid on interest bearing liabilities.

- *Other Operating Income (OOI)*: The OOI of SCBs was projected using the following regression:

$$LOOI_t = -\alpha_1 + \beta_1 \times LOOI_{t-1} + \beta_2 \times LNGDP_SA_t$$

where, α_1, β_1 and $\beta_2 > 0$.

- *Operating Expense (OE)*: The OE of SCBs was projected using the Autoregressive Moving Average (ARMA) model.

- *Provision*: The required provisioning was projected using the following regression:

$$P_Adv_t = \alpha_1 + \beta_1 \times P_Adv_{t-1} - \beta_2 \times RGDP_Gr_{t-2} + \beta_3 \times GNPA_{t-1} - \beta_4 \times Dummy$$

where, $\alpha_1, \beta_1, \beta_2, \beta_3$ and $\beta_4 > 0$, P_Adv is provisions to total advances ratio. RGDP_Gr is the y-o-y growth rate of real GDP. GNPA is gross non-performing advances to total advances ratio. Dummy is a time dummy.

- *Income Tax*: The required income tax was taken as 32 per cent of profit before tax, which is based on the past trend of ratio of income tax to profit before tax.

Impact of GNPA on capital adequacy

Finally, impact on CRAR was estimated based on the PAT estimated as mentioned earlier. RWA growth was assumed at 10 per cent under the baseline, 12.5 per cent under medium risk and 15.5 per cent under severe risk scenarios. Regulatory capital growth was assumed to remain at the minimum by assuming minimum mandated transfer of 25 per cent of the profit to the reserves account. The projected values of the ratio of the non-performing advances were translated into capital ratios using the 'balance sheet approach', by which capital in the balance sheet is affected via provisions and net profits.

Single factor sensitivity analysis – Stress testing

As a part of quarterly surveillance, stress tests are conducted covering credit risk, interest rate risk, liquidity risk etc. and the resilience of commercial banks in response to these shocks is studied. The analysis is done on individual SCB as well as on the aggregated-system.

Credit risk

To ascertain the resilience of banks, the credit portfolio was given a shock by increasing GNPA levels for the entire portfolio as well as for few select sectors. For testing the credit concentration risk, default of the top

individual borrower(s) and the largest group borrower was assumed. The analysis was carried out both at the aggregate level as well as at the individual bank level. The assumed increase in GNPA was distributed across sub-standard, doubtful and loss categories in the same proportion as prevailing in the existing stock of NPAs. However, for credit concentration risk the additional GNPA under the assumed shocks were considered to fall into sub-standard category only. The provisioning norms used for these stress tests were based on existing average prescribed provisioning for different asset categories. The provisioning requirements were taken as 25, 75 and 100 per cent for sub-standard, doubtful and loss advances respectively. These norms were applied on additional GNPA calculated under a stress scenario. As a result of the assumed increase in GNPA, loss of income on the additional GNPA for one quarter was also included in total losses in addition to additional provisioning requirements. The estimated provisioning requirements so derived were deduced from banks' capital and stressed capital adequacy ratios were derived.

Interest rate risk

Under assumed shocks of the shifting of the INR yield curve, there could be losses on account of the fall in value of the portfolio or decline in income. These estimated losses were reduced from the banks' capital to arrive at stressed CRAR.

For interest rate risk in the trading portfolio (HFT + AFS), a duration analysis approach was considered for computing the valuation impact (portfolio losses). The portfolio losses on these investments were calculated for each time bucket based on the applied shocks. The resultant losses/gains were used to derive the impacted CRAR. In a separate exercise for interest rate shocks in the HTM portfolio, valuation losses were calculated for each time bucket on interest bearing assets using the duration approach. The valuation impact for the tests on the HTM portfolio was calculated under the assumption that the HTM portfolio would be marked-to-market.

Evaluation of the impact of interest rate risk on the banking book was done through 'income approach'. The impact of shocks were assessed by estimating income losses on the exposure gap of rate sensitive assets and liabilities, excluding AFS and HFT portfolios, for one year only for each time bucket separately. This reflects the impact on the current year profit and loss and income statements.

Liquidity risk

The aim of the liquidity stress tests is to assess the ability of a bank to withstand unexpected liquidity drain without taking recourse to any outside liquidity support. Various scenarios depict different proportions (depending on the type of deposits) of unexpected deposit withdrawals on account of sudden loss of depositors' confidence and assess the adequacy of liquid assets available to fund them. Another liquidity risk analysis based on the unutilised portion of credit lines which are sanctioned/committed/guaranteed (taking into account the undrawn working capital sanctioned limit, undrawn committed lines of credit and letters of credit and guarantees) was carried out to focus on banks' ability to fulfil the additional and sudden demand for credit with the help of their liquid assets only.

Assumptions in the liquidity stress tests include:

- It is assumed that banks will meet stressed withdrawal of deposits or additional demand for credit through sale of liquid assets only.
- The sale of investments is done with a haircut of 10 per cent of their market value.
- The stress test is done on a static mode.

Stress testing of the derivatives portfolios of select banks

The stress testing exercise focused on the derivatives portfolios of a representative sample set of the top 20 banks in terms of notional value of the derivatives portfolios. Each bank in the sample was asked to assess the impact of stress conditions on its respective derivatives portfolio.

In the case of domestic banks, the derivatives portfolios of both domestic and overseas operations were included. In case of foreign banks, only the domestic (Indian) position was considered for the exercise. For derivatives trade where hedge effectiveness was established it was exempted from stress tests, while all other trades were included.

The stress scenarios incorporated four sensitivity tests consisting of the spot USD/INR rate and domestic interest rates as parameters (Table 2).

Table 2: Shocks for Sensitivity Analysis

Domestic Interest Rates		
Shock 1	Overnight	+2.5 percentage points
	Upto 1yr	+1.5 percentage points
	Above 1yr	+1.0 percentage points

Domestic Interest Rates		
Shock 2	Overnight	-2.5 percentage points
	Upto 1yr	-1.5 percentage points
	Above 1yr	-1.0 percentage points

Exchange rates		
Shock 3	USD/INR	+20 per cent

Exchange Rates		
Shock 4	USD/INR	-20 per cent

Scheduled urban co-operative banks**Credit risk**

Stress tests on credit risk were conducted on SUCBs using their asset portfolios as at end September 2014. The tests were based on a single factor sensitivity analysis. The impact on CRAR was studied under four different scenarios. The assumed scenarios were:

- Scenario I: 0.5 SD shock on GNPA (classified into sub-standard advances).
- Scenario II: 1 SD shock on GNPA (classified into loss advances).
- Scenario III: 0.5 SD shock on GNPA (classified into sub-standard advances).
- Scenario IV: 1 SD shock on GNPA (classified into loss advances).

Liquidity risk

A liquidity stress test based on a cash flow basis in the 1-28 days time bucket was also conducted, where mismatch (negative gap [cash inflow less than cash outflow]) exceeding 20 per cent of outflow was considered stressful.

- Scenario I: Cash outflows in the 1-28 days time bucket goes up by 50 per cent (no change in cash inflows).
- Scenario II: Cash outflows in the 1-28 days time bucket goes up by 100 per cent (no change in cash inflows).

Non-banking financial companies

Credit risk

Stress tests on credit risk were conducted on non-banking financial companies (including both deposit taking and non-deposit taking and systemically important) using their asset portfolios as at end September 2014. The tests were based on a single factor sensitivity analysis. The impact on CRAR was studied under two different scenarios:

- Scenario I: GNPA increased by 0.5 SD from the current level.
- Scenario II: GNPA increased by 1 SD from the current level.
- Scenario III: GNPA increased by 3 SD from the current level.

The assumed increase in GNPA was distributed across sub-standard, doubtful and loss categories in the same proportion as prevailing in the existing stock of GNPA. The additional provisioning requirement was adjusted from the current capital position. The stress test was conducted at individual NBFCs levels as well as at an aggregate level.

Interconnectedness: Network analysis

Matrix algebra is at the core of the network analysis, which is essentially an analysis of bilateral exposures between entities in the financial sector. Each institution's lendings and borrowings with all others in the system are plotted in a square matrix and are then mapped in a network graph. The network model uses various statistical measures to gauge the level of interconnectedness in the system. Some of the most important ones are:

Connectivity: This is a statistic that measures the extent of links between the nodes relative to all possible links in a complete graph.

Cluster Coefficient: Clustering in networks measures how interconnected each node is. Specifically, there should be an increased probability that two of a node's neighbours (banks' counterparties in case of the financial network) are also neighbours themselves. A high clustering coefficient for the network corresponds with high local interconnectedness prevailing in the system.

Shortest Path Length: This gives the average number of directed links between a node and each of the other nodes in the network. Those nodes with the shortest path can be identified as hubs in the system.

In-betweenness Centrality: This statistic reports how the shortest path lengths pass through a particular node.

Eigenvector Measure of Centrality: Eigenvector centrality is a measure of the importance of a node (bank) in a network. It describes how connected a node's neighbours are and attempts to capture more than just the number of out degrees or direct 'neighbours' that a node has. The algorithm assigns relative centrality scores to all nodes in the network and a bank's centrality score is proportional to the sum of the centrality scores of all nodes to which it is connected. In general, for a NxN matrix there will be N different eigen values, for which an

eigenvector solution exists. Each bank has a unique eigen value, which indicates its importance in the system. This measure is used in the network analysis to establish the systemic importance of a bank and by far it is the most crucial indicator.

Tiered Network Structures: Typically, financial networks tend to exhibit a tiered structure. A tiered structure is one where different institutions have different degrees or levels of connectivity with others in the network. In the present analysis, the most connected banks (based on their eigenvector measure of centrality) are in the innermost core. Banks are then placed in the mid-core, outer core and the periphery (the respective concentric circles around the centre in the diagrams), based on their level of relative connectivity. The range of connectivity of the banks is defined as a ratio of each bank's in degree and out degree divided by that of the most connected bank. Banks that are ranked in the top 10 percentile of this ratio constitute the inner core. This is followed by a mid-core of banks ranked between 90 and 70 percentile and a 3rd tier of banks ranked between the 40 and 70 percentile. Banks with a connectivity ratio of less than 40 per cent are categorised as the periphery.

Solvency contagion analysis

The contagion analysis is basically a stress test where the gross loss to the banking system owing to a domino effect of one or more banks failing is ascertained. We follow the round by round or sequential algorithm for simulating contagion that is now well known from Furfine (2003). Starting with a trigger bank i that fails at time 0, we denote the set of banks that go into distress at each round or iteration by D_q , $q = 1, 2, \dots$. For this analysis, a bank is considered to be in distress when its core CRAR goes below 6 per cent. The net receivables have been considered as loss for the receiving bank.

Liquidity contagion analysis

While the solvency contagion analysis assesses potential loss to the system owing to failure of a net borrower, liquidity contagion estimates potential loss to the system due to the failure of a net lender. The analysis is conducted on gross exposures between banks. The exposures include fund based and derivatives ones. The basic assumption for the analysis is that a bank will initially dip into its liquidity reserves or buffers to tide over a liquidity stress caused by the failure of a large net lender. The items considered under liquidity reserves are: (a) excess CRR balance; (b) excess SLR balance; (c) available marginal standing facility; and (d) available export credit refinance. If a bank is able to meet the stress with liquidity buffers alone, then there is no further contagion.

However, if the liquidity buffers alone are not sufficient, then a bank will call in all loans that are 'callable', resulting in a contagion. For the analysis only short-term assets like money lent in the call market and other very short-term loans are taken as callable. Following this, a bank may survive or may be liquidated. In this case there might be instances where a bank may survive by calling in loans, but in turn might propagate a further contagion causing other banks to come under duress. The second assumption used is that when a bank is liquidated, the funds lent by the bank are called in on a gross basis, whereas when a bank calls in a short-term loan without being liquidated, the loan is called in on a net basis (on the assumption that the counterparty is likely to first reduce its short-term lending against the same counterparty).